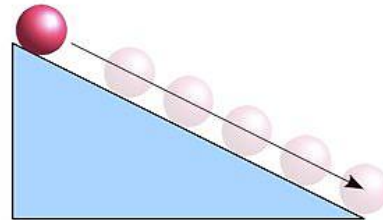


Lesson 6: Solving Basic One-Variable Quadratic Equations

Classwork

Example 1

A physics teacher put a ball at the top of a ramp and let it roll down toward the floor. The class determined that the height of the ball could be represented by the equation $h = -16t^2 + 4$, where the height, h , is measured in feet from the ground and time, t , in seconds.



- What do you notice about the structure of the quadratic expression in this problem? How can this structure help us when we apply this equation?
- In the equation, explain what the 4 represents.
- Explain how you would use the equation to determine the time it takes the ball to reach the floor.
- Now consider the two solutions for t . Which one is reasonable? Does the final answer make sense based on this context? Explain.

Exercises

Solve each equation. Some of them may have radicals in their solutions.

1. $3x^2 - 9 = 0$

2. $(x - 3)^2 = 1$

3. $4(x - 3)^2 = 1$

4. $2(x - 3)^2 = 12$

5. Analyze the solutions for Exercises 2–4. Notice how the questions all had $(x - 3)^2$ as a factor, but each solution was different (radical, mixed number, whole number). Explain how the structure of each expression affected each problem-solution pair.
6. Peter is a painter and he wonders if he would have time to catch a paint bucket dropped from his ladder before it hits the ground. He drops a bucket from the top of his 9-foot ladder. The height, h , of the bucket during its fall can be represented by the equation, $h = -16t^2 + 9$, where the height is measured in feet from the ground, and the time since the bucket was dropped, t , is measured in seconds. After how many seconds does the bucket hit the ground? Do you think he could catch the bucket before it hits the ground?

Lesson Summary

By looking at the structure of a quadratic equation (missing linear terms, perfect squares, factored expressions), you can find clues for the best method to solve it. Some strategies include setting the equation equal to zero, factoring out the GCF or common factors, and using the zero product property.

Be aware of the domain and range for a function presented in context, and consider whether answers make sense in that context.

Problem Set

1. Factor completely: $15x^2 - 40x - 15$.

Solve each equation.

2. $4x^2 = 9$

3. $3y^2 - 8 = 13$

4. $(d + 4)^2 = 5$

5. $4(g - 1)^2 + 6 = 13$

6. $12 = -2(5 - k)^2 + 20$

7. Mischief is a toy poodle that competes with her trainer in the agility course. Within the course, Mischief must leap through a hoop. Mischief's jump can be modeled by the equation $h = -16t^2 + 12t$, where h is the height of the leap in feet and t is the time since the leap, in seconds. At what values of t does Mischief start and end the jump?